



A tidal force is a difference in the strength of gravity between two points. The gravitational field of the moon produces a tidal force across the diameter of Earth, which causes the Earth to deform. It also raises tides of several meters in the solid Earth, and larger tides in the liquid oceans.

If the tidal force is stronger than a body's cohesiveness, the body will be disrupted. The minimum distance that a satellite comes to a planet before it is shattered this way is called its Roche Distance. The artistic image to the left shows what tidal disruption could be like for an unlucky moon.

A human falling into a black hole will also experience tidal forces. In most cases these will be lethal! The difference in acceleration between the head and feet could be many thousands of Earth Gravities. A person would literally be pulled apart! Some physicists have termed this process spaghettification!

$$a = \frac{2GM}{R^2} \frac{d}{R}$$

Problem 1 - The equation lets us calculate the tidal acceleration across a body with a length of  $d$ . The acceleration of gravity on Earth's surface is  $979 \text{ cm/sec}^2$ . The tidal acceleration between your head and feet is given by the above formula. For  $M$  = the mass of Earth ( $5.9 \times 10^{27}$  grams),  $R$  = the radius of Earth ( $6.4 \times 10^8$  cm) and the constant of gravity whose value is  $6.67 \times 10^{-8}$ , calculate  $a$  if  $D = 2$  meters.

Problem 2 - What is the tidal acceleration across the full diameter of Earth?

Problem 3 - A stellar-mass black hole has the mass of the sun ( $1.9 \times 10^{33}$  grams), and a radius of 2.8 kilometers. A) What would be the tidal acceleration across a human at a distance of 100 kilometers? B) Would a human be spaghettified?

Problem 4 - A supermassive black hole has 100 million times the mass of the sun ( $1.9 \times 10^{33}$  grams), and a radius of 280 million kilometers. What would be the tidal acceleration across a human at a distance of 100 kilometers from the event horizon of the supermassive black hole?

Problem 5 - Which black hole could a human enter without being spagettified?

**Answer Key:**

Problem 1 - The equation lets us calculate the tidal acceleration across a body with a length of  $d$ . The acceleration of gravity on Earth's surface is  $979 \text{ cm/sec}^2$ . The tidal acceleration between your head and feet is given by the above formula. For  $M$  = the mass of Earth ( $5.9 \times 10^{27}$  grams),  $R$  = the radius of Earth ( $6.4 \times 10^8$  cm) and the constant of gravity whose value is  $6.67 \times 10^{-8}$ , calculate  $a$  if  $D = 2$  meters.

$$\begin{aligned} \text{Answer: } a &= 2 \times (6.67 \times 10^{-8}) \times (5.9 \times 10^{27}) \times 200 / (6.4 \times 10^8)^3 \\ &= 0.000003 \times (200) \\ &= 0.0006 \text{ cm/sec}^2 \end{aligned}$$

Problem 2 - What is the tidal acceleration across the full diameter of Earth?

$$\text{Answer: } D = 6.4 \times 10^8 \text{ cm, so } a = 0.000003 \times 6.4 \times 10^8 = 1,920 \text{ cm/sec}^2$$

Problem 3 - A stellar-mass black hole has the mass of the sun ( $1.9 \times 10^{33}$  grams), and a radius of 2.8 kilometers. A) What would be the tidal acceleration across a human at a distance of 100 kilometers? B) Would a human be spaghettified?

$$\begin{aligned} \text{Answer: } a &= 2 \times (6.67 \times 10^{-8}) \times (1.9 \times 10^{33}) \times 200 / (1.0 \times 10^7)^3 \\ &= 50,700,000 \text{ cm/sec}^2 \end{aligned}$$

Yes, this is equal to  $50,700,000/979 = 51,700$  times the acceleration of gravity, and a human would be pulled apart and 'spaghettified'

Problem 4 - A supermassive black hole has 100 million times the mass of the sun ( $1.9 \times 10^{33}$  grams), and a radius of 280 million kilometers. What would be the tidal acceleration across a human at a distance of 100 kilometers from the event horizon of the supermassive black hole?

$$\begin{aligned} \text{Answer: } a &= 2 \times (6.67 \times 10^{-8}) \times (1.9 \times 10^{41}) \times 200 / (2.8 \times 10^{13})^3 \\ &= 0.00023 \text{ cm/sec}^2 \end{aligned}$$

Problem 5 - Which black hole could a human enter without being spaghettified?

Answer: Yes, the tidal force is far less than what a human normally experiences on the surface of Earth.